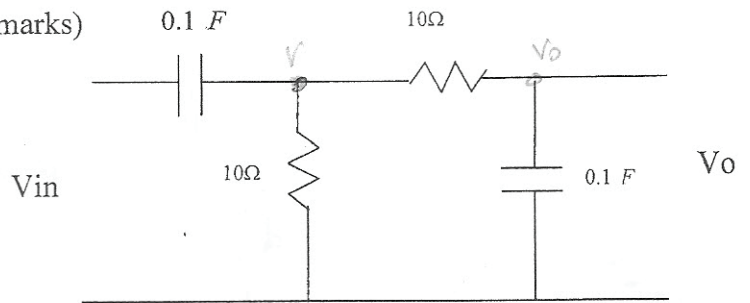


11.5
20

Question #1 (6 mark)

For circuit shown find:

- 1- Transfer function $H(j\omega) = V_o(j\omega)/V_{in}(j\omega)$ (3-marks)
- 2- Kind of filter (1-marks)
- 3- Cutoff frequency/ies (2- mark)



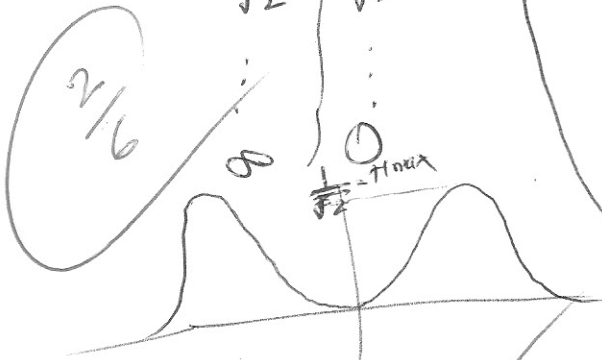
$$H(j\omega) = \frac{V_o(j\omega)}{V_{in}(j\omega)}$$

$$H(j\omega) = \frac{\frac{j\omega}{20}}{\frac{100}{40} + j\omega - 5\omega^2}$$

$$|H(j\omega)| = \frac{\frac{\omega}{2}}{\sqrt{(\omega^2 + (\frac{10}{1} - 5\omega^2))^2}}$$

$$\angle H(j\omega) = \frac{\pi}{2} - \tan^{-1}$$

ω	$ H $
0	0
\dots	\dots
$\frac{1}{\sqrt{2}}$	$\frac{1}{\sqrt{2}}$
\dots	\dots
∞	0



② the kind is Band Pass filter

$$\omega_{C1/2} = \frac{R}{2L} \pm \sqrt{\left(\frac{R}{2L}\right)^2 + \frac{1}{LC}}$$

$$H(j\omega) = \frac{H_{max}}{\sqrt{2}} = \frac{1}{\sqrt{2}} = \frac{1}{2} \rightarrow$$

$$5/2 - 5\omega_c^2 = 1$$

$$\text{node V: } \frac{V - V_{in}}{0.1F} + \frac{V}{10\Omega} + \frac{V - V_o}{10\Omega} = 0$$

$$V = V_{in} \frac{10}{10 + 0.1F}$$

$$V_o = V \frac{0.1F}{0.1F + 10 + 10}$$

$$V_o = V_{in} \frac{10}{10 + 0.1F} \cdot \frac{0.1F}{0.1F + 20} \rightarrow \frac{1}{j\omega C} = \frac{10}{j\omega}$$

$$\frac{V_o}{V_{in}} = \frac{\frac{20}{j\omega} \cdot \frac{10}{j\omega}}{\frac{20}{j\omega} + 200 + \frac{100}{(j\omega)^2} + \frac{20}{j\omega}}$$

$$= \frac{20 j\omega}{\frac{100}{\omega^2} + 40j\omega + 200} \cdot j\omega^2$$

to find ω_c

$$\frac{\frac{1}{2} \omega}{\sqrt{\omega^2 + (\frac{5}{2} - 5\omega^2)^2}} = \frac{1}{2}$$

$$\frac{\frac{1}{4} \omega^2}{\omega^2 + (\frac{5}{2} - 5\omega^2)^2} = \frac{1}{4}$$

$$1 \omega^2 = \omega^2 + (\frac{5}{2} - 5\omega^2)^2 \rightarrow \omega_c^2 = \frac{1}{2} \therefore \omega_c = \frac{1}{\sqrt{2}}$$

Question # 2 (6 mark)

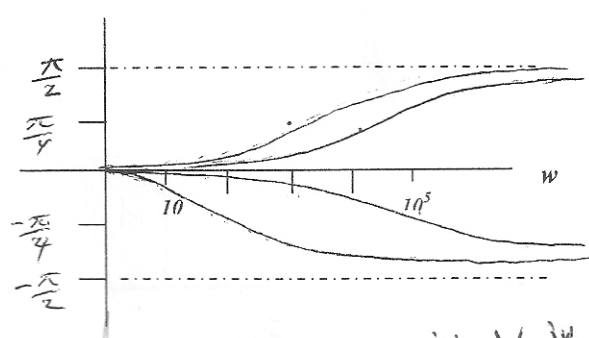
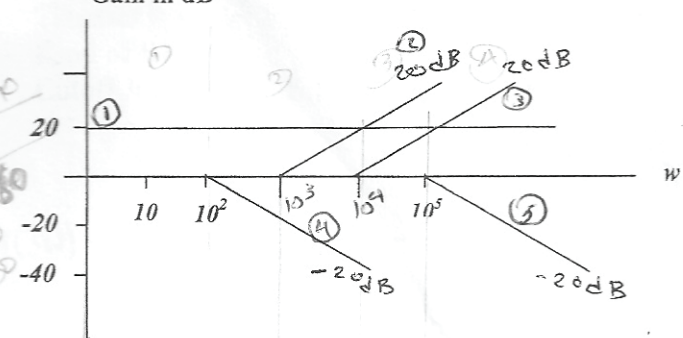
a) Ascertain has filter consist of 5 sections as shown in the following bode diagrams find:

- Total magnitude and phase diagrams (3-marks)
- If $V_{in}(t) = 10 \sin(200t) + 10 \sin(2000t) + 10 \sin(20000t)$ write an expression for $V_o(t)$ (2-marks)
- What is the bandwidth of the filter (1-mark)

Gain in dB

phase

① $20 \rightarrow W+20$
 $-W+20$
 $20 \rightarrow W-20$
 $-W+20$



① $20 \text{ dB} = 20 \log_{10} K = 20 \log_{10} 10 \Rightarrow K = 10$

② $1 \text{ dB} = 20 \log_{10} \frac{W}{10^3} \Rightarrow \frac{W}{10^3} + 1 = H(jW)$

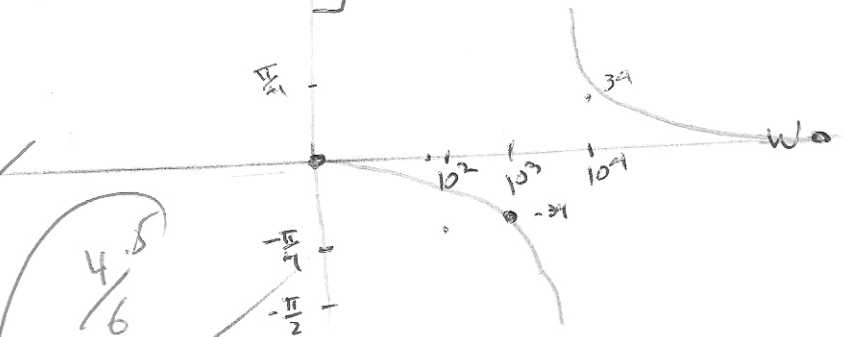
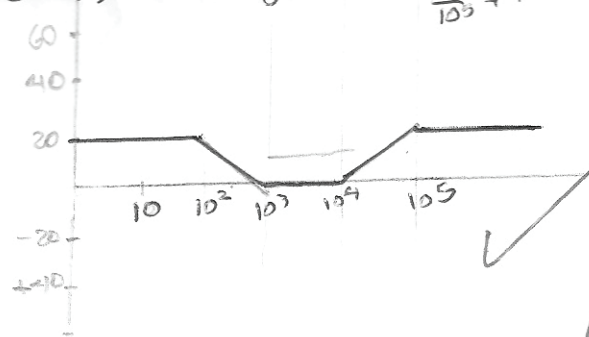
③ $1 \text{ dB} = 20 \log_{10} \frac{W}{10^4} \Rightarrow \frac{W}{10^4} + 1 = H(jW)$

④ $1 \text{ dB} = -20 \log_{10} \frac{W}{10^2} \Rightarrow \frac{1}{\frac{W}{10^2} + 1} = H(jW)$

⑤ $1 \text{ dB} = -20 \log_{10} \frac{W}{10^5} \Rightarrow \frac{1}{\frac{W}{10^5} + 1} = H(jW)$

$$H(jW) = \frac{10 \left(\frac{jW}{10^3} + 1 \right) \left(\frac{jW}{10^5} + 1 \right)}{\left(\frac{jW}{10^2} + 1 \right) \left(\frac{jW}{10^4} + 1 \right)}$$

$$\angle H(jW) = 0 + \tan^{-1} \frac{W}{10^3} + \tan^{-1} \frac{W}{10^5} - \tan^{-1} \frac{W}{10^2} - \tan^{-1} \frac{W}{10^4}$$



$W = 2 \times 10^2$
 $\text{dB} \approx 20$
 $20 = 20 \log_{10}(\text{gain})$
 $\text{gain} = 10^1 = 10$
 $\theta = -34^\circ$

$W = 2 \times 10^3$
 $\text{dB} \approx 0$
 $0 = 20 \log_{10}(\text{gain})$
 $\text{gain} = 10^0 = 1$
 $\theta = -34^\circ$

$W = 2 \times 10^4$
 $\text{dB} = 0$
 $0 = 20 \log_{10}(\text{gain})$
 $\text{gain} = 10^0 = 1$
 $\theta = 34^\circ$

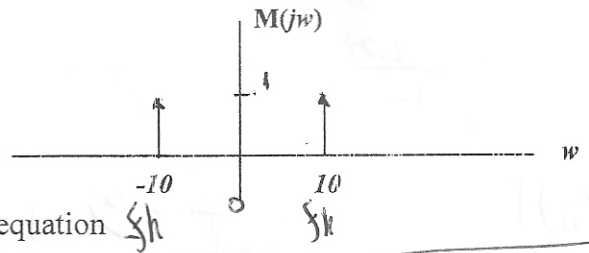
$$V_o(t) = 10(10) \sin(200t - 34^\circ) + 10(1) \sin(2000t - 34^\circ) + 10(1) \sin(20000t + 34^\circ)$$

$$BW = W_{c2} - W_{c1} = 10^4 - 10^3 = 9000$$

Question # 3 (8 mark)

a) A certain signal $m(t)$ has the following spectrum is sampled by sampling frequency 20 rad/sec

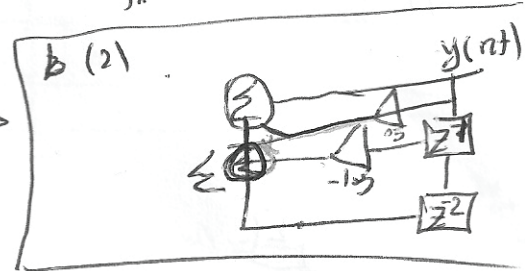
- 1- sketch the sampled frequency
- 2- if the sampled frequency applied to ideal LPF with cutoff 10 rad/sec sketch the output of the filter
- 3- if the signal sampled with frequency 15 rad/sec what is the output of low pass filter



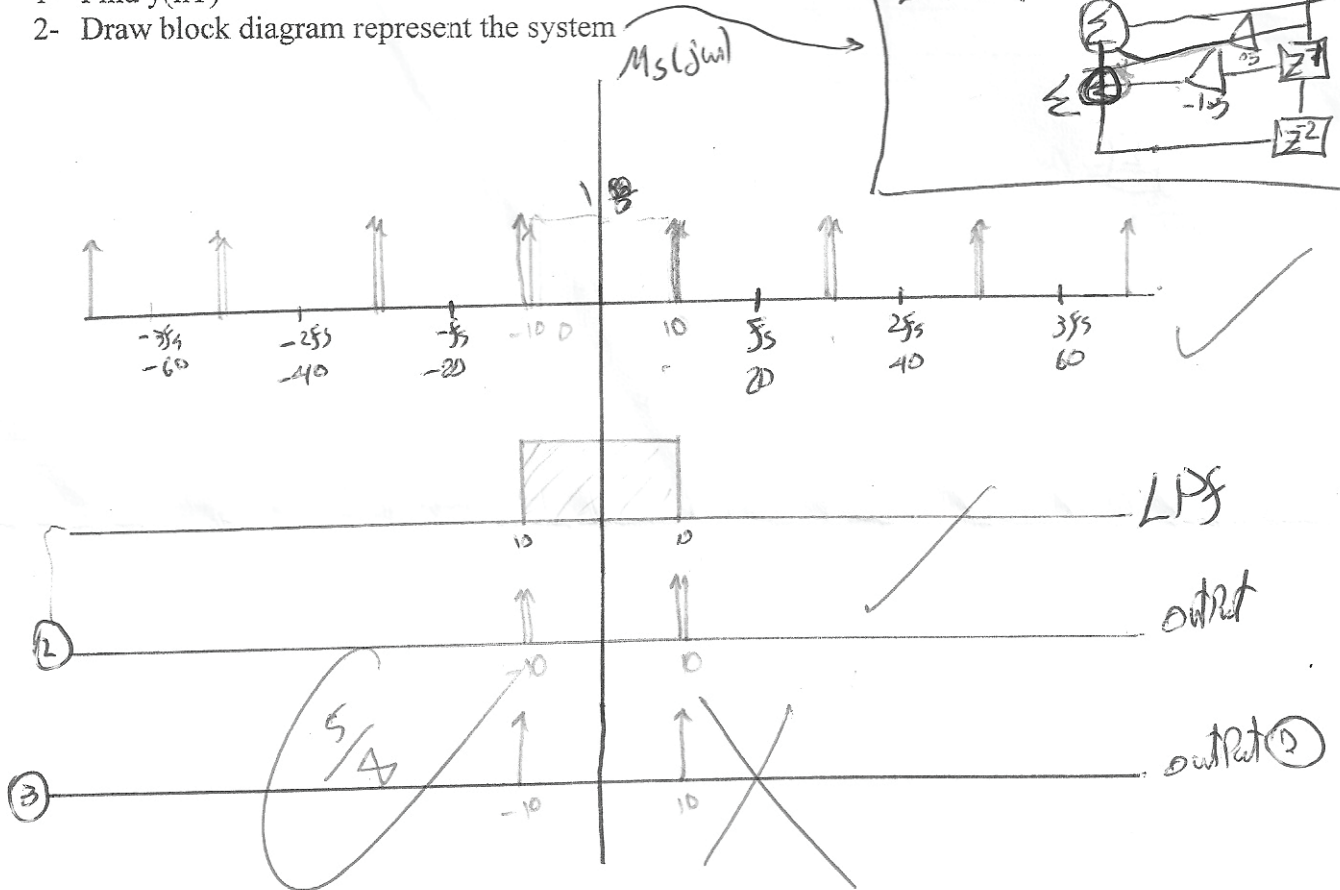
b) A certain discrete system represent by the following equation

$$y(n-2] - 1.5 y[n-1] + 0.5 y[n] = (0.25)^n$$

- 1- Find $y[nT]$
- 2- Draw block diagram represent the system



(a)



(b) ① transform to $Y(z)$:

$$Y(z)z^{-2} - 1.5Y(z)z^{-1} + 0.5Y(z) = \frac{1}{1 - 0.25z^{-1}}$$

$$Y(z)[z^{-2} - 1.5z^{-1} + 0.5] = \frac{1}{1 - 0.25z^{-1}}$$

$$\therefore Y(z) = \frac{1}{[z^{-2} - 1.5z^{-1} + 0.5][1 - 0.25z^{-1}]} = \frac{z^2}{(0.5z^2 - 1.5z + 0.5) [1 - 0.25z^{-1}]}$$

$$= \frac{z^2}{(z-2)(z-1)} \cdot \frac{1}{1 - 0.25z^{-1}} = \frac{1}{(1-2z^{-1})(1-z^{-1})(1-0.25z^{-1})}$$

$$= \frac{A}{1-2z^{-1}} + \frac{B}{1-z^{-1}} + \frac{C}{1-0.25z^{-1}} \Rightarrow A(1-z^{-1})(1-0.25z^{-1}) + B(1-2z^{-1})(1-0.25z^{-1}) + C(1-2z^{-1})(1-z^{-1}) = 1$$

$$A \Big|_{z=\frac{1}{2}} = \frac{1}{(1-\frac{1}{2})(1-0.25(\frac{1}{2}))} = 2.28$$

$$B \Big|_{z=1} = \frac{1}{(1-2)(1-0.25)} = -0.75$$

$$C \Big|_{z=\frac{1}{0.25}} = \frac{1}{1-2(\frac{1}{0.25})(1-\frac{1}{0.25})} = 0.04$$